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# PARAMETERS INFLUENCING BOND STRENGTH OF REBARS IN REINFORCED CONCRETE

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#### ABSTRACT

This paper discusses experimental investigations on bond stress-slip response in concrete in end anchorages of steel reinforcement. The influence of embedment length, bar diameter and lateral confinement on the end anchorage bond strength, and bond stress-slip response has been studied. Twenty four anchorage pull-out specimens provided with two embedment lengths 50mm and 150mm and two different bar diameters 16mm and 20mm with three types of lateral confinements. The compressive strength of concrete used in this study was 50 MPa. The bond strength of reinforcing bars in concrete decreases with increasing the embedment length. Relatively brittle failures have been observed in members with large embedment length. Further, the bond strength of larger diameter bars decreases as compared with smaller diameter bars. The plain concrete pullout specimens exhibited concrete splitting failures, while the presence of lateral confinement altered the failure from concrete splitting to pullout of rebars. The lateral confinement increases the bond strength and the length of post-peak stress-slip response, thus showing the improvement of ductility.

Keywords: Concrete, Bond Strength

# **INTRODUCTION**

The behaviour of reinforced concrete (RC) structures depends up on the type of bond developed between the steel reinforcement and the surrounding concrete. Bond stress is the tangential shear or friction developed between the reinforcement and the surrounding concrete that transfers the force onto the reinforcement. To ensure the integrity of various constituent or composite action of concrete and steel reinforcement, sufficient bond should be developed by the surrounding concrete with the reinforcement. Proper bond between the steel reinforcement and the surrounding concrete is also crucial for the overall strength and serviceability of RC members. The failure of RC structures may be due primarily to the deterioration of the bond. Hence, while modeling an RC member for inelastic dynamic analysis, the slip of the rebars in the interior beam-column joints needs to be considered (ACI 352, 1985).

#### **Review of Literature**

Bond in RC members depends on type of bar, state of stress in both bar and concrete, strength of concrete, concrete cover, confinement, space between adjacent bars, number of layers of reinforcement bars, position of reinforcing bars, and casting direction. The type of cracking leading to failure has been investigated using deformed bars in tension by injecting ink around the bars (Rehm, 1961; Goto, 1971). The bond strength of rebars in concrete decreases as the embedment length increases, and decreases with increasing the bar diameter (Mathey and Watstein, 1961). The previous investigations proved that the bond strength of rebars in concrete is influenced by the development length rather than the bar diameter (Ferguson et al., 1962). The ultimate bond strength seems to be a function of  $\sqrt{f_c}$  when other parameters

are constant, since the bond strength is related to the tensile strength of concrete. Studies on understanding the nature of bond, modes of failure and factors influencing the failure, bar spacing and beam width, end anchorage, flexural bond and anchorage bond with high strength ribbed bars have been reported (Ferguson et al., 1966). The slip of deformed bars is due to (i) splitting of concrete by wedge action, and (ii) crushing of concrete in front of the ribs (Rehm, 1961; Lutz and Gergely, 1967).

Nilson (1972) used slope of steel strain curve to evaluate the bond stress at a given load in reinforcing bar, and a new test method was adopted to study the local slip, secondary cracking and strain distribution in

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concrete (Jiang et al., 1984). A bond stress-slip model has been proposed to predict the load end slip and anchorage length of bars extended from adjoining beams in to exterior columns under large nonlinear actions (Ueda and Hawkins, 1986). Effect of bar diameter, confinement and strength of concrete on the bond behaviour of bar hooks in exterior beam-column joints has been reported (Soroushian, 1988). The bond strength decreases as the bar diameter increases. The post-peak bond-slip response was not influenced by the bar diameter (Soroushian and Choi, 1989), while confinement has direct influence on the local bond stress (Soroushian et al., 1991). A new bond stress-slip response has been simulated recently by Abrishami and Mitchel (1992). However, consistent bond stress-slip response was obtained on short embedment length (Malvar, 1992). A mathematical model for bond stress-slip response of a reinforcing bar due to cyclic load has been reported (Yankelevsky et al., 1992). Other models to predict the tensile strength of concrete from the pullout load has been reported (Bortolotti, 2003). Confinement by ordinary steel reinforcement has improved the bond strength with significant ductility (Harajli et al., 2004). Several studies on bond in normal strength concrete (NSC) have been reported (Jian et al., 1984: Somayaji and shah, 1981). In high strength concrete (HSC), increasing the development length does not seem to increase the bond strength of deformed bars when the concrete cover is relatively small. A minimum confinement reinforcement needs to be provided over the splice length in RC members when HSC is used (Azizinamini et al., 1993, Azizinamini et al., 1999a). An expression has been proposed to estimate the extra confinement reinforcement (Azizinamini et al., 1999b). The bond strength decreases slightly with increase in the bar diameter, while the frictional resistance does not depend on the bar diameter, lug spacing or relative rib area (Eligehausen et al., 1983). More general information on the local bond can be seen (CEB-FIP Report, 2000).

### **Research Significance**

Significant research efforts have been made on anchorage bond in normal strength concrete (NSC). However, a bond strength and its model need to be developed for HSC members since HSC RC members tend to fail in brittle manner. Further, there is a need to re-evaluate the design requirements in the codes of practice vis-à-vis crack widths and spacing, deflection, rotation capacity, anchorage and splice length, to propose new test procedures and assessment criteria for bond strength of bars incorporating various influencing parameters and with modified surface characteristics. This study attempts to investigate the influence of embedment length on bond strength and bond stress-slip response in RC members with high strength deformed bars for varying bar diameter and confinement.

# Development Length in Codes of Practice

For design purpose, the codes of practice recommend provisions for development length of rebars in concrete in terms of the mean bond stress. The design equations provide development length necessary to achieve the full yield strength of reinforcement bar. The minimum embedded length required to develop the yield strength of the rebar is known as the development length. However, the bond stress is an important factor for the development of stresses in the reinforcing bars. ACI code (ACI 318-2005) provisions for development length stipulate an upper limit of concrete compressive strength of 69 MPa. The reason for this upper limit is due to lack of confirmed test data on HSC. The development length of rebar at a critical section can be estimated by,

(1)

$$l_{d} = \frac{9}{10} \frac{f_{y}}{\sqrt{f_{c}}} \frac{\psi_{t} \psi_{e} \psi_{s} \lambda}{\left(\frac{c_{b} + K_{tr}}{d_{b}}\right)} d_{b}$$

Where,

 $d_b = Diameter of bar$   $\delta = light weight aggregate factor$   $\psi_t = top bar effect factor$   $\psi_e = coating effect factor$   $\psi_s = rebar size factor$  $C_b = Cover to reinforcement bar$ 

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 $K_{tr} = Transverse reinforcement index$ 

 $\dot{f}_c$  = Strength of concrete

 $f_y =$  Yield strength of steel

Euro Code 2 (1992) provides a simple expression for estimating the development length of reinforcing bars in concrete in the following form.

$$L_d = \frac{f_{yd} \varphi}{4 f_{bu}} \tag{2}$$

The Indian standard (IS 456–2000) considered the basic development length as a function of yield strength of reinforcement, diameter of rebar. The design bond strength is a function of the compressive strength of concrete as given below

$$L_d = \frac{\phi \sigma_s}{4\tau_{bd}} \tag{3}$$

The development length requirements specified by the codes of practice indicate that the bond strength of rebar in concrete is a variable. However, the provisions by various codes of practice are applicable to conventional strength concretes.

# Local Bond Stress vs. Slip Response

The local bond stress-slip response is characterized by the variation of local bond stress, ' $\tau$ ' with the

corresponding slip, 's'. The bond stress can be described as a power function of slip i.e.  $\tau = a \cdot \Delta^b$ . The constants 'a' and 'b' depend on the type of bar and compressive strength of concrete. The constant 'a' depends on the compressive strength of concrete, f<sub>c</sub> and can be expressed as,  $a = kf_c$ . Few models describe the bond stress as a function of slip alone (Nilson 1972, Mirza and Houde 1979), which are applicable to unconfined concrete with a very small value of slip (s < 0.1mm). The bond strength is a function of compressive strength of concrete. The diameter of the bar is not incorporated in these models. However, the information on bond stress- slip have been limited to conventional concrete. The models proposed by Ciampi *et al.*, (1981, 1982) and Eligehausen *et al.*, (1983) considered the other influencing parameters. As shown in Fig. 1, the bond stress-slip model has three parts. The ascending part of the model is defined by

$$\tau = \tau_1 \cdot \left(\frac{s}{s_1}\right)^{\alpha} \text{ for } 0 \le s \le s_1 \tag{4}$$

The second part is a horizontal plateau at  $\tau_{max} = \tau_1 = \tau_2$  between  $s_1 \le s \le s_2$ , and third part is a linear descending branch starting from bond stress " $\tau_2$ " with slip " $s_2$ " and ending at a residual bond stress " $\tau_3$ " at a slip of " $s_3$ ". The value of " $\alpha$ " is obtained as 0.4 from the regression analysis, for high strength concretes. The ultimate bond strength is  $\tau_1 = 2.5 f_c^{1/2}$ , which overestimates the bond strength of rebar in HSC.





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# MATERIALS AND METHODS

#### Materials

Portland Pozzolanic Cement (PPC) was used for preparation of end anchorage pullout specimens. The natural river sand, and normal weight granite coarse aggregate of 20mm maximum size were used in the concrete. The main steel reinforcement is of high yield strength deformed (HYSD) bar of diameters 16 mm or 20 mm was adopted as anchorage reinforcement. 6mm diameter plain mild steel (MS) bars were used as spiral confinement reinforcement and closed stirrups or rings. The arrangement of longitudinal and lateral reinforcement in pullout specimen is shown in Fig. 1. The concrete mix proportions were 1: 1.64: 3.02: 0.35 with cement content =  $400 \text{ kg/m}^3$  and water-cement ratio = 0.35 for producing 50 MPa compressive strength. Three standard cubes of size 150mm x 150mm x 150mm were also cast along with the anchorage pullout specimen to determine the compressive strength of concrete. *Test Geometry* 

The test specimen was basically a concrete cube 150mmx150mmx150mm with a reinforcement bar embedded coaxially with nominal spiral reinforcement surrounding the bar (IS: 2770-1997). Well seasoned wooden moulds were used to cast the pullout specimens. The main longitudinal reinforcement bars were placed in the horizontal direction. One end of the bar was projected about 15mm to measure the slip of the bar at the free end, while the loaded end was extended up to 750mm in order to grip it in the machine and transfer the force. Typical pullout specimen is shown in Figure 1. The pullout studies were done for two different bar diameters, 16mm and 20mm, to understand the influence of bar diameter on the bond strength with different embedment lengths. To achieve 50mm embedment length at the centre of the pullout specimen, PVC sleeves were covered at the ends to unbond the rebars. The slip was recorded at both the loaded and free ends of the reinforcement bar. After twenty four hours of casting of concrete, the pullout specimens were demolded and cured for 28 days. The main longitudinal bar was embedded with different confinements by spirals and stirrups or ties along with the controlled pullout specimens without confinement.





Figure 1: Arrangement of Reinforcement and typical Pullout specimen

#### **Testing** Procedure

The pullout tests were conducted under displacement control using 250kN capacity actuator. The pullout specimen was accommodated in a steel frame that could be inverted and hung from the actuator. To reduce the frictional resistance of the bearing steel plates on the free movement of concrete specimen, Teflon sheets were placed between the concrete and steel plate of the frame. A load cell along with two linearly variable differential transducers (LVDTs) were mounted with the test specimen to measure the load applied and slip of the two ends of the rebar. Electrical resistant strain gauges were also mounted on the main longitudinal reinforcing bar to measure the strain. The load cell, LVDTs and the strain gauges were connected with a data logger that recorded the readings at a frequency of 0.5Hz continuously. The test set-up and the arrangement of LVDTs are shown in Figure 2. Monotonic loading was transferred through the actuator to the reinforcing bar, and rate of displacement was 1.51mm/min (i.e. 0.025mm/sec). The test was stopped at a slip of 60mm or up to complete pulling out of rebars whichever occurred first to complete the test.

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Figure 2: Test set-up and arrangement of LVDTs

# **RESULTS AND DISCUSSION**

Tests were conducted on twenty four pull-out specimens to understand the influence of various parameters on the bond strength as well as the bond stress vs. slip response. The unconfined concrete surrounding the end region of the main reinforcing bar in tension provided least resistance due to formation of splitting cracks caused by the high tensile hoop stresses. An ideal pull-out failure was observed in all the specimens designed with confinement reinforcement, while splitting failure was observed in the specimens without confinement reinforcement. Wide longitudinal splitting cracks were noticed on the outer surface of the specimen. In the pullout specimens designed with confinement by ties or spirals, the splitting crack formation and their propagation were effectively contained by lateral reinforcement. The effectiveness of confinement depends up on its form. The descending portion of the bond stress-slip response shows the level of deterioration bond stiffness with decreasing pullout load. The concrete occupied between the rebar ribs was sheared off with the confinement and the stresses in the bars were observed to be much less than their yield strength. However, the unconfined concrete exhibited splitting and there were no traces of crushing of concrete in front of the ribs.

#### Bond Stress vs. Slip Response

Slip is the relative displacement of reinforcement bar measured with reference to the surrounding concrete. The total slip of the bar includes the relative slip at the interface and shear deformations in concrete also. Therefore, certain displacement was recorded due to the localized strains at the interface even if there was nonoccurrence of bar slip. Figure 3 shows a typical bond stress vs. slip response in pullout specimens provided with 20mm diameter bar with 150mm embedment length. The interaction between concrete and the reinforcing bar in tension can be characterized through four stages in the bond stress-slip response. The first stage of the response corresponds to the low bond-stress, in which chemical adhesion is predominant. At still higher bond stress levels, the longitudinal splitting cracks propagated radially due to the resulting force component developed by the wedging action of the reinforcing bar ribs.





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By providing the lateral confinement reinforcement, the splitting of concrete was prevented effectively. Subsequently, the force in the reinforcing bar was transferred through friction between the reinforcement and the surrounding concrete. With further increase in the slip of the rebar, the bond stress reached its peak value and then drops. However, the bond stress was not negligible even at the larger slip of the bar. In the descending branch of the bond stress-slip curve, the resistance against the slip was due to dry-friction developed as the concrete keys between the bar ribs were sheared off, and the tips of the ribs offer less wedge action. The lateral reinforcement showed significant influence on the magnitude of slip, relative movement of the concrete between the ribs. The confinement by the lateral reinforcement improved the cracking resistance as well as the load carrying capacity. The cracking distribution was uniform and the failure was gradual. Hence the lateral confinement has improved the shear strength and ductility of anchorage pullout regions.

# **Bond Strength**

The bond stress vs. slip (free end and forced end) response in 50 MPa strength concrete is shown in Figures 4 to 6 with various bar diameters and different lateral confinements. The maximum bond stress,  $\tau_{max}$  has been observed at the rebar slip varying between 0.5 and 1.5 mm in concrete of 50 MPa compressive strength. The bond strength of anchorage pullout plain concrete specimens has been observed to be less than that of the confined concrete, which ranges between 50 and 60% of that of the confined concrete. The bond stress corresponding to the longitudinal splitting was about 11.8 MPa in concrete with compressive strength of 50MPa. After attaining the peak stress, a rapid decrease in the bond stress has been observed. A horizontal plateau has been observed sustaining the maximum bond stress,  $\tau_{max}$  between the slip ranging between 0.3mm and 3.0mm. After the peak stress, the bond stress vs. slip response has been decreased rapidly between the slip varying from 3.0 to 8.2 mm. At the end of the rapid descending branch, the bond resistance has been decreased to  $\tau_3$  or  $\tau_f$  called frictional bond resistance at a slip of about 10mm. Thereafter, the bond strength has been observed to remain constant until failure.



#### Influence of Embedment Length

The maximum bond stress ( $\tau_{max}$ ) of 25.5 MPa was the highest value achieved with 50 mm embedment length using 16mm diameter bar, at a slip, s<sub>1</sub> ranging between 0.3 mm and 1.5 mm as shown in Figure 4. There was no significant variation in the stiffness of the ascending branch as well as the plateau of the bond stress. However, the post-peak response with 50mm embedment length seems to be more ductile compared with 150 mm length as shown in Figures 4 and 5. With 50 mm embedment length, the slip difference (s<sub>3</sub>–s<sub>2</sub>) varied between 3.25 mm to 11.5 mm, while with 150 mm embedment length it was varying between 3.5 mm and 24 mm. The fact is that as the surface area of embedment increases, the

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maximum bond stress decreases. It shows, however, that there exists a size effect on the bond strength. Similar conclusions have been drawn by the earlier researchers that the bond strength decreases as the embedment length increases (Mathey and Watstein, 1961).



Figure 5: Bond stress vs. slip ( $\varphi = 16$ mm,  $l_b = 150$ mm,  $f_c = 50$  MPa)



20 mm rebars with 50mm embedment in 50 MPa concrete

Figure 6: Bond stress vs. slip ( $\phi = 20$ mm,  $l_b = 50$ mm,  $f_c = 50$  MPa)

# Influence of Lateral Confinement

The influence of lateral confinement on the bond strength of rebars in concrete can be demonstrated in Figures 4 to 6. The splitting failure of concrete was prevented by the lateral confinement. The spiral reinforcement improved the bond strength of concrete. However, there appears a limit on the confinement level beyond which the bond strength does not increase substantially. The length of the descending branch of the bond stress-slip curve has been significantly increased with the confinement by spirals. The confinement by spirals has been very effective than the ties. When the embedment length was 50 mm, the performance of ties was similar to that of the spirals. It has been reported earlier that the confinement of concrete influences the local bond stress in deformed bars (Soroushain et al., 1991). By varying the confining ties, consistent bond stress-slip response was achieved with short embedment length (Malvar 1992). Further, confinement with ordinary steel improved the bond strength marginally, while the ductility was improved significantly (Harajli *et al.*, 2004).

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#### Influence of Bar Diameter

The bond strength of rebars does not seem to be increased as its diameter increases. However, using 16mm diameter bar, the maximum bond stress ( $\tau_{max}$ ) was sustained between the bar slip ranging between 0.3mm and 1.5mm. The maximum bond stress ( $\tau_{max}$ ) was achieved at a bar slip ranging from 0.5 mm to 2.0mm with 20mm diameter bars. This shows that the slip at the peak stress was slightly increased with 20mm diameter bars. There has not been much influence of the bar diameter on the range of the bar slip in the horizontal plateau i.e. between the slips  $s_1$  and  $s_2$ . The frictional resistance ( $\tau_f$ ) with 16mm diameter bars varies between 1.0 MPa and 8.0 MPa, while it varies between 2.8 MPa and 10.5MPa using 20mm diameter bars. This indicates that the frictional bond resistance has been slightly high when 20mm diameter bars. The studies by Soroushian (1988) and Mathey and Watstein (1961) on surface deformed bars with different diameters in confined concrete showed that the bond strength decreases as the bar diameter increases. However, the post-peak response and the overall bond-slip response were not influenced by the bar diameter (Soroushian and Choi, 1989). The bond strength decreases with the increasing bar diameter and the frictional bond resistance bar diameter, spacing of rib (Eligehausen *et al.*, 1983).

#### Modeling of Bond Stress-Slip Response

A generic local bond stress-slip model, as shown in Figure 1, has been reported (Eligehausen et al., 1983). This model has five parameters; bond stresses  $\tau_1$  and  $\tau_3$ , and the slip at different stages  $s_1$ ,  $s_2$  and  $s_3$ . These parameters  $s_1$ ,  $s_2$ ,  $s_3$  and  $\tau_3$  are independent of the compressive strength of concrete, confinement of the transverse reinforcement, and the bar diameter. However, the bond stress " $\tau_1$ " depends on the strength of concrete and bar diameter. In the present study, the bond stress-slip models have been studied by varying the diameter of bar, type of confinement and embedment length. The salient points of the model are; maximum bond strength,  $\tau_{max}$  and the corresponding slip,  $s_1$ , the slip at the end of plateau,  $s_2$  and the frictional bond strength,  $\tau_f$  and corresponding slip,  $s_3$ . The model consists of nonlinear portion in the ascending branch up to  $s_1$  and a plateau from slip  $s_1$  to  $s_2$ . The expression for the bond stress of the ascending portion is

$$\tau = \tau_{\max} \left[ \frac{s}{s_{\max}} \right]^{\alpha} \tag{5}$$

Where,  $1.0 \le s_{max} \le 1.2mm$ 

The initial portion of the bond stress-slip response is curvilinear. However, the value of  $\alpha$  tends to be 0.3 when the concrete compressive strength ranges from 40 MPa to 80 MPa, which needs further investigations. The descending branch of the bond stress-slip response is extended up to the bond stress,  $\tau_f$ , and the corresponding slip, s<sub>3</sub>). After slip, s<sub>3</sub>, the bond resistance remains constant at  $\tau_f$  until failure. In concrete specimens without confinement, the mean ultimate bond strength,  $\tau_{max}$  is observed to be 8.35 MPa with the corresponding slip,  $s_1$  of 0.95 mm. The mean slip at the end of plateau,  $s_2$  is 1.50 mm in concrete specimens without confinement. The post-peak response has been observed to be relatively steep without confinement. The value of frictional resistance,  $\tau_f(\tau_3)$  is 1.5 MPa. The slip of the bar at the end of descending branch,  $s_3$  is 5.0 mm. The slip at the end of the test is assumed as 7.5 mm without confinement at a bond stress of 1.5 MPa. For concrete specimens with confinement, the ultimate bond strength,  $\tau_{max}$ has been observed to be 12.30 MPa with the corresponding slip, s1 of 2.0mm. The post-peak response of the bond stress-slip response is gradual with the lateral confinement. The value of the frictional resistance,  $\tau_{\rm f}$  (=  $\tau_3$ ) is 6.5 MPa in concrete with the lateral confinement. The slip at the end of the descending branch,  $s_3$  is 10.0 mm in concrete with lateral confinement. The slip at the end of failure was assumed as 20 mm with the lateral confinement with a bond stress of 6.50 MPa. It appears that the bond strength increases significantly in concrete provided with lateral confinement. At a given bond stress, the slip increases in concrete with lateral confinement. The resisting bond capacity after slip,  $s_3$  is improved by providing the lateral confinement.

#### Lateral Strength of $l_b$ $d_b$ $\tau_{(max)}$ $\mathbf{s}_1$ $s_2$ **S**3 $\tau_{(f)}$ S. No Concrete, MPa Confinement mm MPa MPa mm mm mm mm 1 Ties 50 150 20 14.0 1.0 10.0 4.4 1.8 2 Ties 50 150 16 13.2 0.8 3.8 7.5 7.2 3 Spirals 50 12.8 4.3 7.5 50 20 1.3 10.5 4 Spirals 50 150 16 10.8 0.5 2.0 9.3 5.0 5 Ties 50 50 20 9.2 1.5 3.0 9.0 4.4 UC\* 6 50 150 16 8.4 0.5 0.8 4.8 1.0

#### Table 1: Bond stress and other parameters for modeling of bond stress-slip response

\* unconfined concrete

Table 2: Typical Anchorage bond model parameters in concrete
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Parameter	Unconfined Concrete	Confined Concrete
S <sub>1</sub>	0.95	2.0
$S_2$	1.50	7.5
$S_3$	5.0	10.0
α	0.3	0.3
$ au_{\mathbf{f}}$	$0.18 au_{max}$	$0.5\tau_{max}$

#### **Conclusions**

From the experimental results, the following conclusions can be drawn

1. The maximum bond strength of rebar in concrete without lateral confinement ranges between 50 and 60 % of that of the laterally confined concrete. The splitting of concrete occurs in plain concrete, and the bond strength drops to zero suddenly after the splitting of concrete.

2. The lateral confinement ensures the development of full bond strength, which results in an ideal pullout rebars. The rebars confined with spiral reinforcement showed increase in the bond strength and improvement in the ductility.

3. The bond strength of rebars decreases as its embedment length increases. The influence of bar diameter on the local bond stress-slip is not clear in the range ( $d_b = 16$  and 20mm) of diameters used.

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